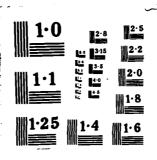
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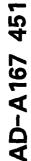


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DEPARTMENT OF DEFENCE DEFENCE SCIENCE AND TECHNOLOGY ORGANISATION AERONAUTICAL RESEARCH LABORATORIES

MELBOURNE, VICTORIA

Structures Technical Memorandum 424

A COMPUTER PROGRAM FOR CALCULATING THE STEADY AND OSCILLATORY SUPERSONIC FLOW OVER THIN WINGS

by

I. A. GRAR

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SUMMARY

A computer program for the calculation of linearised steady and oscillatory supersonic flow over thin wings has been implemented on the ELXSI. The program uses an explicit finite difference scheme on a characteristic grid to solve for the reduced potential and pressure coefficient on the wing surface.



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NOTATION

Symbol	Definition
AME	final Mach number
AMS	initial Mach number
AOME	final reduced frequency
AOMS	initial reduced frequency
вг	semi span length
C(i,j,k)	f(i,j-1, k-1) + f(i,j-1, k+1) + f(i,j+1, k-1) + f(i,j+1, k+1)
c _p	steady pressure coefficient
DAM	delta change in Mach number
DAOM	delta change in reduced frequency
DX	characteristic grid spacing
f	reduced steady/oscillatory velocity potential
r̃(i,j,k)	$(1-p) f(i,j,k) + \frac{p}{2} [f(i+1, j, k) + f(i-1, j, k)]$
FXL (Y)	position of the leading edge
FXT (Y)	position of the trailing edge
h	vertical position of wing surface
h _o	oscillatory part of wing surface
h _s ±	steady upper/lower position of wing
H1 (X,Y)	$h_0/h_s^+_X$ for oscillatory/steady flow
H2 (X,T)	h_{OX}/h_{S-X}^{-} for oscillatory/steady flow
IOUT	output parameter
ISW	option parameter
k	WM/α ²
K	k/zero for oscillatory/steady flow
1	typical chord length

NOTATION (CONT.)

Symbol	Definition
М	free stream Mach number
M(i,j,k)	f(i,j-1,k) + f(i,j+1,k) + f(i,j,k-1) + f(i,j,k+1)
p	constant/local pressure
P _∞	free stream pressure
Q	oscillatory pressure coefficient
υ _∞	free stream velocity
x,y,z,t	Eulerian variables
α	√ M ² -1
δ	thickness ratio
Δ	rectangular grid step length
η,ζ,τ	Prandtl-Glauert variables
λ	constant
ρ∞	free stream density
ф	perturbation potential
Ф _О	oscillatory perturbation potential
ф _в	steady perturbation potential
Ф	sealed oscillatory perturbation potential
ψ	velocity potential
ω	reduced frequency

INTRODUCTION

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A computer program for the calculation of steady and oscillatory supersonic flow over thin wings has been implemented in Fortran on the ELXSI. As the basic differential equation is 'time-like' and the relevant part of the flow-field finite, the program uses an explicit finite-difference scheme to solve for the reduced potential on the wing.

In section 2 the governing differential equations and boundary conditions for steady and oscillatory supersonic flow over a thin wing are developed, and in section 3 the explicit finite difference formula applicable to linearised supersonic flow is presented. This formula has the advantage of using a characteristic grid rather than a rectangular grid thus halving the number of grid points. The method is restricted to boundary conditions defined on a plane. Section 4 discusses how to use the program, that is; setting up the data, compiling, binding and running. A listing of the program is given in Appendix A and finally a listing of a subroutine to read the output from the supersonic program is given in Appendix B, this subroutine is discussed in Section 4.

2. GOVERNING EQUATION AND BOUNDARY CONDITIONS

In the following, the isentropic inviscid flow of a perfect gas, initially irrotational, is considered. Thus we may assume the existence of a velocity potential ψ , such that the fluid velocity $\underline{v} = \underline{v}\psi$. If U is the free stream velocity (which is assumed to be directed solely in the x- direction), then a perturbation potential ϕ can be defined such that

$$\psi(x,y,z,t) = U^{\infty} \left[x + \phi(x,y,z,t) \right], \tag{1}$$

where x,y,z represent a rectangular carterian co-ordinate system and t is the time variable. Note that subsequent equations are expressed in non-dimensional co-ordinates based on a length scale 1, a typical value of the airfoil chord length, a velocity scale U_{∞} and a density scale 1_{∞} , a typical value of the density at infinity. The time variable is then scaled with 1_{∞} and the pressure with 1_{∞} 1_{∞}

For thin nearly planar wings of moderate aspect ratio the governing differential equation for the perturbation velocity potential can be written as

$$(M^2 - 1) \phi_{xx} - \phi_{yy} - \phi_{zz} + 2M^2 \phi_{xt} + M^2 \phi tt = 0,$$
 (2)

where M is the free stream Mach number. It should be noted here that the procedure used to derive (2) is based upon the small parameter δ representing the ratio of airfoil thickness to chord length. It is assumed that as $\delta \to 0$, ϕ/δ remains fixed. Then ignoring terms of second order in δ , we find that (2) is the appropriate governing differential equation for ϕ .

On a surface in an inviscid fluid the usual kinematic condition applies. If Z = h(x,y,t) specifies the wing (where h is under δ by definition), then, to first order in δ , the boundary condition on the wing is

$$\phi_{z} /_{z=0} = \frac{\partial h}{\partial x} + \frac{\partial h}{\partial t} . \tag{3}$$

In many practical applications the unsteady motion of a wing may be assumed to consist of small infiniterimal perturbations around the steady state configuration. Thus the motion consists of a steady component plus a small harmonically oscillating unsteady component. Let

$$\phi$$
 (x,y,z,t) = ϕ_S (x,y,z) + ϕ_O (x,y,z) e^{inet}, (4a)

$$h(x,y,t) = h_S^{\pm}(x,y) + h_O(x,y) e^{inet},$$
 (4b)

where, the subscript S/O denotes the steady/oscillatory part, $h_{S}^{\,\pm}$ represents the upper/lower surface of the wing and due to the sealings introduced above, ω represents the reduced frequency or Stroubal number. Note that the actual frequency is ω U / 2. Substituting (4a and b) into (2) and (3), and separating steady and oscillatory parts we find that

$$(M^2 -1) \phi_{SXX} = \phi_{SYY} + \phi_{SZZ}, \qquad (5a)$$

$$\phi_{SZ} / z=0 = \frac{\partial}{\partial x} h_x^{\pm}$$
 on the wing, (5b)

and
$$(M^2 - 1)$$
 $\phi_{OXX} + z_i \omega M^2 \phi_{OX} - M^2 \omega^2 \phi_{O}$

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(6a)

$$\phi_{OZ} / z=0$$
 = $\frac{\partial h_{O}}{\partial x}$ + $i\omega h_{O}$ on the wing. (6b)

At this stage it is convenient to introduce the generalised $Prandtl-Glauert\ variables$

$$\eta = \alpha y$$
, $\zeta = az$ and $\tau = a^2 t/m$ (7a)

where
$$a^2 = M^2 -=1 >0.$$
 (7b)

Also, in order to write (6a) in canonical form let

$$\phi_{O} = \phi(x,\eta,\zeta) \quad e^{-i\,kmx}, \tag{8a}$$

where

$$k = \omega M/\alpha^2.$$
 (8b)

Substituting (7a and b) into (5a and b), and, (7a and b) and (8a and b) into (6a and b) the steady and oscillatory problems become

$$\phi_{SXX} = \phi_{S\eta\eta} + \phi_{S\zeta\zeta}, \tag{9a}$$

$$\phi_{S\zeta/\zeta = 0\pm} = \frac{1}{\alpha} h_S^{\pm} \times \text{ on the wing}$$
 (9b)

and

Carlo Maria Carlo Control Control

$$\Phi_{xx} + k^2 \Phi = \Phi_{\eta\eta} + \Phi_{\zeta\zeta},$$
 (10a)

$$\Phi_{\zeta/\zeta=0} = \frac{e^{i kmx}}{\alpha} (h_{ox} + i\omega_{ho})$$
 on the wing. (10b)

Finally note that if k is zero then the partial differential equation (10a) reduces to the saw form as (9a). Also the boundary conditions (9b) and (10b) have similar forms. Due to these similarities both the steady and oscillatory problems can be solved by the same finite difference technique. In the next section we discuss the finite difference scheme that will be used to solve both (9a,b) and (10a,b).

3. FINITE DIFFERENCE SCHEME

The basic equation of linearised supersonic flow is

$$f_{xx} + K^2 f = f_{yy} + f_{zz}$$
 (11)

where x is the flow direction, f the reduced perturbation velocity potential and K is a frequency parameter for unsteady flow, or zero for steady flow.

Let the potential be defined at grid points forming a cubic lattice at which it may be assumed that the co-ordinates take integer values (i,j,k). It has been shown by Sullivan [1] that a second order, consistent, finite difference scheme, with rotational symmetry about the x-axis and which reduces to the method of characteristics for two-dimensional flow in the x-y or x-z planes, is

$$f(i+1,j,k) + f(i-1,j,k) + K^{2}\Delta^{2} \tilde{f}(i,j,k)$$

$$= -\lambda f(i,j,k) + \frac{\lambda}{2} M(i,j,k) + (\frac{1}{2} - \frac{\lambda}{4}) C(i,j,k)$$
 (12a)

where

$$\tilde{f}(i,j,k) = (1-p) f(i,j,k) + \frac{1}{2} P [f(i+1,j,k) + f(i-1,j,k)],$$
 (12b)

$$M(i,j,k) = f(i,j-1,k) + f(i,j+1,k) + f(i,j,k-1)$$

+ $f(i,j,K+1)$, (12c)

$$C(i,j,k) = f(i,j-1,k-1) + f(i,j+1,k-1) + f(i,j-1,k+1) + f(i,j-1,k+1),$$
 (12d)

where P and λ are constants and Δ is the grid step-length. It has also been shown by Sullivan [1] that the two-parameter family of finite difference schemes (12a,b,c and d) are strictly stable in the range

$$1 \ge \lambda 0$$
 , $p \ge \frac{1}{2}$. (13)

Following Sullivan [1] choose the simplest scheme $\,\lambda$ = 0, p = 1 giving:

$$f(i+1,j,k) + f(i-1,j,k) = \frac{-1}{(2+K^2\Lambda^2)} C(i,j,k).$$
 (14)

Note that (14) has the advantage that the terms f(i,j,k) and M(i,j,k) do not appear, giving a reduction in the number of grid points required. That is, the system (14) is solved on a characteristic grid rather than a rectangular grid.

Note that (14) is neutrally stable. This neutral stability will manifest itself as numerical instability as the number of grid points downstream becomes large.

Normal derivative boundary conditions can be implemented in a variety of ways. The technique used with (14) is to generate dummy potentials using the known normal derivates, with grid points on the boundary treated as interior points. That is

$$fz / z=0 = [f(i,j,2) - f(i,j,0)] / 2\Delta,$$
 (15)

then on the boundary, level k = 1, (14) becomes

$$f(i+1,j,1) + f(i-1,j,1)$$

$$= \frac{2}{(2+K^2\Delta^2)} \left[f(i,j-1,2) + f(i,j+1,2) - \Delta f_z(i,j-1) - \Delta f_z(i,j+1) \right].$$
 (16)

4. DISCUSSION

The supersonic program solves accurately the partial differential equations derived in Section 2. However, we should note that the equations (9a,b) and (10a,b) are approximate representations of the flow about a thin wing. Thus the numerical results should be viewed as approximations to the flow, though the results should be reasonably accurate, provided the thickness parameter δ , is small and the Mach number is not too close to unity.

The program offers a resolution of up to 291 x 291 grid points on the x-y plane. From experience with the program 50 x 50 grid points gives excellent agreement (i.e. four significant figures) with the assymptotic solutions for an infinite rectangular wing, at various Mach numbers and a sonic triangular wing.

It should be stated that the program uses very little central processing time. When the functions are given by Table 1 and the data by Table 2 (i.e. the sonic triangular wing) the running time is 7.2 c.p.u. seconds. If the grid step length is halved, that is put DX equal to 0.01, then the running time is 30.6 c.p.u seconds. Also, note that binding takes about six c.p.u. seconds.

Finally note that the program is capable of handling quite elaborate wing planforms. For instance; forward swept wings and wings with monotonically curved or convex leading and trailing edges; however, the program will in most cases be unable to determine the proper grid system for wings with more than one extreme leading or trailing point.

REFERENCE

[1] M.C.W. SULLIVAN, "Explicit finite difference methods for linearised oscillatory supersonic flow" British Aerospace,

BAe - KSD - R - GEN - 1155, August 1983.

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TABLE 1: Example of function subroutines FXL(Y), FXT(Y), HI(X,Y) and H2(X,Y)

FUNCT.F

REAL FUNCTION FXL(Y)
FXL=Y
RETURN

Alternate entry for fxt.
ENTRY FXT(Y)
FXT=1.0
RETURN
END

REAL FUNCTION H1(X,Y)
PARAMETER (PI=3.1415926)
DATA THETA/0.5/
H1=-1.0*X*TAN(THETA*PI/180.0)
RETURN

C Entry for h2.
ENTRY H2(X,Y)
H2=-1.0*TAN(THETA*PI/180.0)
RETURN
END

3

- -

TABLE 2: Example of input data for supersonic program.

The first two parameters have Fortran format type 12, while, the rest have format type F12.8

TEST1.D

1 3 0.02	I SW I OUT
0.02	DX B2
1.4142196	AMS
1.4142196	AME DAM
0.1	AOMS
0.1 0.1	AOME DAOM

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TABLE 3: Example of output when the functions in Figure 1 and the input data of Figure 2, are used

SONIC1.D

--

Unsteady supersonic.

Grid step size = .20000E-01 Semi span length = 1.0000

.10000 Initial Mach no. = 1.41422 Final Mach no. = 1.41422 Mach no. step =

Initial freq. = .10000 Final freq. = .10000 Freq. step = .10000

--

20

Mach No. =1.41422 Frequency = .10000

y = .0100 Points = \$0 x .0100 .02000 .05000 Phi: .0000+000 .1745-003 .054-003 .0000+000 .7958-012 -.1745-006 -.

-tc

APPENDIX A

SUPERSONIC.F

```
PROGRAM SUPERSONIC
COMMON /SUPER/ AL,DX,B2,GS,AM,IM,JC
EXTERNAL FXL,FXT,H1,H2
INTEGER 1S(291),1E(291),JS(291,291),JE(291,291)
DIMENSION XL(581),XT(581),XX(291)
COMPLEX G(581,146),F(291,291),FG(291),ADUM
CHARACTER*4 CH1(4),CH2(4)
DATA CH1/'Phi'',Q"',Phi','Cp
PARAMETER (N=291,N2=581,N3=146)
FORMAT (2(12/),8(F12.8/))
FORMAT(11',5X,'2',/,5X,'Steady supersonic.',//)
FORMAT(1',5X,'2',/,5X,'Steady supersonic.',//)
FORMAT(1',5X,'3',/,5X,'Steady supersonic.',//)
FORMAT(1',5X,'3',1,5X,'Steady supersonic.',//)
FORMAT(1',5X,'1,5X,'Steady supersonic.',//)
FORMAT(1',5X,'1,5X,'Steady supersonic.',//)
FORMAT(1',5X,'1,5X,'Steady supersonic.',//)
Main program for supersonic flow over a thin airfoil.
 46
   47
   48
49
                     Main program for supersonic flow over a thin airfoil.
                                                                                   for unsteady supersonic flow
for steady supersonic flow (unsymmetric)
for steady supersonic flow (symmetric)
                     Output para. IOUT determines type of output; IOUT = 1 for pressure coefficient only, IOUT = 2 for potential only, IOUT = 3 for both potential and pressure.
                   DX = step size, B2 = semi span length
AMS = initial Mach no., AME = final Mach no.
DAM = delta Mach no.
If ISW = 1 then AOMS = initial freq., AOME = final freq.
and DAOM = delta freq..
Leading /trailing edge data is in FXL/FXT.
H1 represents either ho or d/dx.hs+.
H2 represents either d/dx.ho or d/dx.hs-.
                                 READ(5,41,ERR=70,END=71)ISW,IOUT,DX,B2,AMS,AME,DAM,AOMS,AOME,DAOM
GO TO 71
CONTINUE
STOP ' Error in input data.'
CONTINUE
IF (AMS.LE.1.0.OR.AME.LE.1.0) STOP ' Invalid Mach no. range.'
IF (ISW.LT.1.OR.ISW.GT.3) STOP ' Invalid switch parameter in
input data.'
IF (ISW.EQ.1) PRINT 42
IF (ISW.EQ.2) PRINT 43
IF (ISW.EQ.2) PRINT 44
PRINT 45,DAS,AMS,AME,DAM
IF (ISW.EQ.3) PRINT 46,AOMS,AOME,DAOM
DUM=AME-AMS
IF (ISW.EQ.1) PRINT 46,AOMS,AOME,DAOM
DUM=AME-AMS
IF (OUM.NE.0.0) DAM=SIGN(DAM,DUM)
AM=AMS
70
71
                                73
74
75
                                   CALL SOLVE(ISW.N.N2,N3,JS,JE,AK,XL,XT,F,G)
CALL OUTPUT(N,N2,XL,XT,XX,F,18,1E,AK)
```

SUPERSONIC.F

```
IC=4-lABS(5-2*ISW)
IF (IOUT.EQ.1) GO TO 77
DO 76 J=1,JC
IF (IE[J).LT.IS(J)) GO TO 76
Y=FLOAT(2*J-1)*DX/AL/2.0
ITT=1E(J)-1S(J)+1
NUM=INT(FLOAT(ITT+8)/9.0)
IF (NUM.EQ.0) GO TO 76
PRINT 48,Y,ITT
DO 76 I=1,NUM
JB=(I-1)*9*IS(J)
JT=MIN(IE(J),I*9*IS(J)-1)
PRINT 50,CH1(IC),(REAL(F(K,J)),K=JB,JT)
IF (ISW.NE.3) PRINT 50,CH2(IC),(AIMAG(F(K,J)),K=JB,JT)
NNTINUE
CONT.INUE
CONT.INUE
IF (IOUT.NE.1) PRINT 47
ALC=CMPLX(0.0,-2.0*AOM*DX)
DO 7 I=1,JC
IF (IE[J).LE.IS(J)+1. GO TO 79
DO 78 I=IS(J)+1,IE(J)-1
FG(I)=(F(I-1,J)-F(I+1,J)+ADUM*F(I,J))/DX
CONTINUE
Y=FLOAT(2*J-1)*DX/AL/2.0
ITT=IE(J)-IS(J)-1
NUM=INT(FLOAT(ITT+8)/9.0)
PRINT 48,Y,ITT
DO 79 I=1,NUM
JB=(I-1)*9*IS(J)+1
JT=MIN(IE(J)-1,I*9*IS(J))
PRINT 49,(XX(K),K=JB,JT)
PRINT 49,(XX(K),K=JB,JT)
IF (ISW.NE.3) PRINT 50,CH2(IC),(AIMAG(FG(K)),K=JB,JT)
CONTINUE
CONTINUE
IF (ISW.NE.3) PRINT 50,CH2(IC),(AIMAG(FG(K)),K=JB,JT)
IF (ISW.NE.3) PRINT 50,CH2(IC),(AIMAG(FG(K)),K=JB,JT)
CONTINUE
IF (ISW.NE.1) GO TO 81
76
78
79
80
                        CONTINUE
IF (ISW.NE.1) GO TO 81
AOM=AOM+DAOM
IF (DUM2*(AOM-AOME).LE.O.O.AND.DUM2*DAOM.NE.O.O) GO TO 74
                         CONTINUE
IF (DAM
81
                         CUNITNUE
IF (DAM.EQ.0.0) STOP ' Mach no. step size is zero.'
AM=AM+DAM
IF (DUM*(AM-AME).LE.0.0.AND.DUM.NE.0.0) GO TO 72
STOP ' Normal completion.'
                        SUBROUTINE GRIDXY(N,N2,XL,XT,IS,IE,JS,JE)
COMMON/SUPER/ AL,DX,B2,GS,AM,IM,JC
INTEGER IS(N),IE(N),JS(N,N),JE(N,N)
DIMENSION XL(N2),XT(N2)
                     Subroutine to initialize grid system.
                    FIND EXTREME FORWARD AND TRAILING POINTS
Leading and trailing edge data is in function subroutines
FXL and FXT (in Eulerian co-ordinates).
                      DO 900 J=1,N2
    XL(J)=0.0
    XT(J)=0.0
    CONTINUE
    D2=DX/AL/2.0
    JJS=1
    GS=FXL(D2)
    GE=FXT(D2)
    XL(2)=G8
    XT(2)=GE
    J=2
    J=4
    J=4
    J=FLOAT(J-1)*D2
    IF (Y.GT.B2)
    XS=FXL(Y)
    XL(J)=XS
    XT(J)=XS
    XT(J)=XS
    XT(J)=XS
    XT(J)=XS
    XT(J)=XS
    XT(J)=XS
    XT(J)=XS
900
901
```

```
SUPERSONIC.F
```

```
902
  903
000
          Find leading edge/characteristic grid points.
               IS(JJS)=1
IF (JJS.NE.1) THEN
DO 906 J=JJS-1,1,-1
IS(J)=IS(J+1)+1
DUM=XL(2*J)/DX+2.0
CONTINUE
IF (DUM.LE.FLOAT(IS(J))) THEN
IS(J)=IS(J)-1
GO TO 905
END IF
CONTINUE
END IF
  905
  906
                       CONTINUE
IF
(JJS.NE.JC) THEN
DO 908 J=JJS+1,JC
IS(J)=IS(J-1)+1
DUM=XL(2*J)/DX+2.0
CONTINUE
IF (DUM.LE.FLOAT(IS(J))) THEN
IS(J)=IS(J)-1
GO TO 907
END IF
CONTINUE
  907
               END IF
CONTINUE
END IF
  908
             Find trailing edge/characteristic grid points.
               IE(JJE)=1+INT((GE-GS)/DX)
IF (JJE.NE.1) THEN
DO 910 J=JJE-1.1.-1
IE(J)=IE(J+1)-1
DUM=XT(2*J)/DX
CONTINUE
IF (DUM.GE.FLOAT(IE(J))) THEN
IE(J)=IE(J)+1
GO TO 909
END IF
  909
  910
                END IF
                END IF

IF (JJE.NE.JC) THEN

DO 912 J=JJE+1,JC

IE(J)=IE(J-1)-1

DUM=XT(2*J)/DX

CONTINUE

IF (DUM.GE.FLOAT(IE(J))) THEN

IE(J)=IE(J)+1

GO TO 911

END IF

CONTINUE

END IF

J=JC+1

J=J-1

IF (IE(J),LT.IS(J)) GO TO 919
  9:1
```

```
SUPERSONIC.F
              JC=J
000
          FIND TIP DIAPRAGHM REGION
                 J=[NT((IE(JC)-15(JC))/2.0)
              JM=JC+IJ

JM=JC+IJ

IF (IJ.LE.0) G0 T0 918

D0 913 J=JC+1 JM

IS(J)=IS(J-I)+1

IE(J)=IE(J-I)-1
   913 CONTINÚE
0000
         Find j-starting and stopping grid points at all vertical levels.
             IM=IE(JJE)
   DO 916 I=1, IM
    JSW=1
   J=0
   J=J+JSW
   IF (J.GT.JM.OR.J.LT.1) GO TO 916
   IF (I.LT.IS(J).OR.I.GT.IE(J)) GO TO 914
   IF (JSW.EQ.-1) GO TO 915
   JS(1,I)=2*J
   JSW=-1
   J=JM+1
   GO TO 914
   JE(1,I)=2*J
CONTINUE
DO 917 K=2, IM
   K1=K-1
   IK=MOD(K,2)
   DO 917 I=1, IM-K+1
   JS(K,I)=JS(K1,I-IK+1)+2*IK-1
   JE(K,I)=MIN(JE(K1,I),JE(K1,I+1))+1
CONTINUE
RETURN
END
   918
   914
              END
              SUBROUTINE SOLVE(ISW,N,N2,N3,JS,JE,AK,XL,XT,F,G)
COMMON/SUPER/ AL,DX,B2,GS,AM,IM,JC
INTEGER JS(N,N),JE(N,N)
COMPLEX F(N,N),G(N2,N3),DUM,DUM2
DIMENSION XL(N2),XT(N2)
000000
            Subroutine to initialise wing boundary conditions, grid points and integrate the unsteady/steady supersonic problem.
            Initialize boundary conditions.
            ELSE

F(I,JJ)=DD*CMPLX(H1(X,Y),0.0)

END IF

CONTINUE

D0 499 I=1,IM

D0 499 J=JS(1,I),JE(1,I),2

J=J/2

CONTINUE

CONTINUE
  499
```

~ 一大人の日本をある人をあっ

APPENDIX A (CONT.)

```
SUPERSONIC.F
        Initialize integration points to zero.
        D0 550 I=1,N2
D0 550 J=1,N3
G(I,J)=CMPLX(0.0,0.0)
CONTINUE
      Integrate the unsteady and steady supersonic problem.
         ISTOP=2*IM-1
         II=0
II=II+1
KE=IM-IABS(II-IM)
 551
          IK=(II+1)/2
D0 552 J=JS(1,IK),JE(1,IK),2
J1=J+1
         ĎÔ
         J1=J+1

J2=J-1

G(J,Ki)=COEF*(G(J1,K1)+G(J2,K1)+G(J1,K2)+G(J2,K2))-G(J,K1)

CONTINUE

I1=II+1

IF (II.GT.ISTOP) RETURN

KE=IM-IABS(II-IM)

D0 554 K=2,KE,2

K1=K/2

K2=K+1

IK=(II-K+2)/2

D0 554 J=JS(K,IK),JE(K,IK),2

J1=J+1

J2=J-1

IF (J.EQ.i) J2=2

G(J,K1)=COEF*(G(J1,K1)+G(J2,K1)+G(J1,K2)+G(J2,K2))-G(J,K1)

CONTINUE

GO TO 551

END
 553
 554
         930
```

SUBREAD.F

```
SUBROUTINE SUPDAT(M,N,DX,B2,ISW,IOUT,IC,AM,AOM,JC,JP,IP1,IP2,#Y1,Y2,X1,X2,F,G,*)
DIMENSION YI(M,N),Y2(M,N),X1(M,N,N),X2(M,N,N),AM(M),AOM(M)
INTEGER IPI(M,N),IP2(M,N),JC(M),JP(M)
COMPLEX F(M,N,N),G(M,N,N)
FORMAT(6X,II)
FORMAT(6X,II)
FORMAT(4(/),28X,E10.5,29X,F6.4,9(/),7X,I3,3X,I1,//,12X,F7.5,#17X,F7.5)
FORMAT(4(/),28X,E10.5,29X,F6.4,7(/),7X,I3,3X,I1,//,12X,F7.5)
FORMAT(7X,5X,F9,44,18X,I4)
FORMAT(7X,9(F8.5,4X,:))
FORMAT(7X,9(E11.4,1X,:))
FORMAT(7X,13,//,12X,F7.5,17X,F7.5)
FORMAT(7X,I3,//,12X,F7.5,17X,F7.5)
 424445
44748
4748
                                                                    TU=1
READ(1,40,ERR=29)ISW
IF (ISW.EQ.1) READ(1,41,ERR=29)DX,B2,JC(1),IOUT,AM(1),AOM(1)
IF (ISW.NE.1) READ(1,42,ERR=29)DX,B2,JC(1),IOUT,AM(1)
CONTINUE
IF (IOUT.EQ.1) GO TO 24
                                                          IF (15W.NE.1) READ(1,41,ERR=27)DX,B2,JC(1);IOUT,AM(1);AOM(1)
IF (10UT.EQ.1) GO TO 24
DO 23 J=1,JC(1C)
READ(1,43,ERR=29)Y2(1C,J),ITT
NUM=INT(FLOAT(ITT+8)/9.0)
IP2(IC,J)=ITT
DO 23 K=1,NUM
IS=K*9-8
IE=MIN(ITT,K*9)
READ(1,45,ERR=29)(X2(IC,I,J),I=IS,IE)
READ(1,45,ERR=29)(REAL(F(1C,I,J)),I=IS,IE)
READ(1,45,ERR=29)(REAL(F(1C,I,J)),I=IS,IE)
CONTINUE
IF (IOUT.EQ.2) GO TO 26
READ(1,46)
CONTINUE
DO 25 J=1,JC(IC)
READ(1,43,END=28,ERR=29)Y1(IC,J),ITT
IF (ITT.LE.0) GO TO 27
NUM=INT(FLOAT(ITT+8)/9.0)
IP1(IC,J)=ITT
JP(IC)=J
DO 25 K=1,NUM
IS=K*9-8
IE=MIN(ITT,K*9)
READ(1,44,ERR=29)(X1(IC,I,J),I=IS,IE)
READ(1,44,ERR=29)(REAL(G(IC,I,J)),I=IS,IE)
CONTINUE
READ(1,47)
CONTINUE
CONTIN
   22
23
   24
25
26
 27
                                                                      IC=IC+1
IF (IC.GT.M)
IF (ISW.EQ.1)
IF (ISW.NE.1)
GO TO 22
CONTINUE
                                                                                                                                                                                                                                                                               GO TO 30

READ(1,48,END=30,ERR=29)JC(IC),AM(IC),AOM(IC)

READ(1,49,END=30,ERR=29)JC(IC),AM(IC)
30
                                                                  CONTINUE
IC=IC-1
CONTINUE
CLOSE(1)
RETURN
CONTINUE
CLOSE(1)
RETURN
1
END
28
29
```

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APPENDIX C

Description of Computer Program

A computer program based on the finite difference scheme (14) and (16) has been implemented in Fortran on the ARL ELXSI computer. The program consists of a main program called SUPERSONIC and three subroutines, GRIDXY, SOLVE and OUTPUT. For completeness a listing is supplied in Appendix A. The position of the leading and trailing edge, and, either, h_0 and h_{0X} or h_{0X}^{+} and h_{0X}^{-} must be supplied by the user in function subroutines called FXL(Y), FXT(Y), H1(X,Y) and H2(X,Y). For an example see Table 1. Note that X and Y in these functions are sealed Eulerian variables and not Prandtl - Glauert variables.

The program has three options; unsteady flow, steady flow and steady symmetric flow (i.e. hs = - hs x). For unsteady flow H1(x,y) and H2(x,y) represent h_0(x,y) and h_0x(x,y) respectively. The output for the unsteady case is the real and imaginary parts of $\varphi_0(x,y,o)$ (see (4a)) and Q(x,y,o), where the unsteady pressure coefficient is defined as

$$\frac{(P-P_{\infty})}{\frac{1}{2}\rho_{\infty}U_{\infty}^{2}} = Q(x,y,o) \quad e^{i\omega t}.$$
 (17)

For the steady case H1 and H2 represent $h_s^+ x$ and $h_s^- x$. The output for this case is

$$\phi_{\mathbf{S}}$$
 (x,y,o⁺), $\phi_{\mathbf{S}}$ (x,y,o⁻), $C_{\mathbf{p}}$ (x,y,o⁺) and $C_{\mathbf{p}}$ (x,y,o⁻),

where in the steady case,

$$\frac{(P - P_m)}{\frac{1}{2} P_m U_m^2} = C_p (x, y, o^{\pm}).$$
 (18)

APPENDIX C (CONT.)

For the steady symmetric case, the flow below the x-y plane equals the flow above. The output for this case is just ϕ_S (x,y,o⁺) and C_p (x,y,o⁺).

After FXL, FXT, H1 and H2 have been programmed, compile the functions with optimiser switch off, that is

FORTRAN MYFUNCTIONS

-OPT.

Then bind the programs in the following way:

BIND /USER/ST. GEAR/SUPERSONIC, MYFUNCTIONS
BFILE = MY TITLE.

The executable file will then be called MYTITLE and it will exist in your area. To run SUPERSONIC, extra data must be supplied through an input file. Table 2 shows a typical example of the data required by SUPERSONIC.

The first parameter in Table 2 (ISW) has format type I2 and takes the values 1, 2 or 3. That is ISW equals one for unsteady flow, two for steady flow and three for steady symmetric flow. The second parameter IOUT also has format type I2 and it also takes the values 1,2 or 3. It represents the type of output. For instance if IOUT equals one then only the pressure coefficient is output. If IOUT equals two then only the potential is printed. If IOUT is three then both the potential and pressure coefficient are printed. The third parameter DX has format type

F12-8, it determines the distance between grid points on the characteristic grid. Note that DX is twice Δ (see (12a)). When FXL and FXT are given as in Figure 1, the Mach number is $\sqrt{2}$ and DX = 0.02 as in Table 2, then the grid system on the x-y plane has 50 x 50 points. Note that SUPERSONIC can take a grid size on the x-y plane of up to 291 x 291 Also note that if an "ACCESS VIOLATION" error occurs while running SUPERSONIC, then the grid size is greater than 291 x 291 points. To remedy this situation simply increase DX. The fourth parameter B2 also has format type F12.8, it represents the sealed Eulerian semi-span length. The fifth, sixth and seventh parameters determine the initial, final and delta change in Mach number. That is AMS is the initial Mach number, AME is the final Mach number and DAM is the delta change in Mach number. Thus with a suitable choice of AMS, AME and DAM, SUPERSONIC will produce data for several different Mach numbers, during one run. that AMS, AME and DAM have format type F12.8. Also note that if AMS and AME are less than or equal to one, then SUPERSONIC will not execute. The last three parameters are only used if ISW equals 1. AOMS represents the initial reduced frequency, AOME the final reduced frequency and DAOM the delta change in reduced frequency. AOMS, AOME and DAOM have format type

APPENDIX C (CONT.)

F12.8. Note that for each Mach number AOMS, AOME and DAOM determine a range of reduced frequencies. Also note that if ISW is not equal to one then these parameters need not be supplied.

Once the input data have been programmed into a file called, for instance, MYDATA, then SUPERSONIC can be executed by entering:

MYDATA > MYTITLE > MYOUTPUT,

where MYOUTPUT represents the file to which the output is printed. Note that if there is an error in the input data SUPERSONIC will stop execution and print one of three statements. For instance; "invalid switch parameter in input data", signifies that ISW is not in the range one to three, "invalid Mach no. range", signifies that AMS or AME is less than or equal to one, or "error in input data", signifies an error condition was encountered during the input operation. If SUPERSONIC executes normally then upon termination SUPERSONIC prints "normal completion" to your terminal or log file.

Table 3 shows the first part of the output produced when the functions of Table 1 and the data of Table 2 are used. The first character on the first line is a Fortran carriage control character the second character is ISW, in this case 1. DX and B2 are printed on the sixth line, AMS, AME and DAM are printed on the eighth line and if ISW = 1then AOMS, AOME and DAOM are printed on the tenth line. On the twelfth line (or tenth if ISW F 1) the first character is a Fortran carriage control character. The next character is the number of grid points in the y direction, while the last character on this line is IOUT, in this case 3. SUPERSONIC then prints the Mach number and the reduced frequency for the first run, followed by the value of y at the grid points nearest the wing root and the number of points in the x- direction at that value of y, in this case 50. SUPERSONIC then prints the value of x, and the real and imaginary parts of ϕ (or ϕ and ϕ) at each grid point for that y station. After all 50 points have been printed the program then prints the values of x and ϕ at the next value of y until the wing tip is reached. In this case as IOUT equals three the pressure coefficient at each grid point (where it is calculated) is printed in the same way as described above. Note that as the program uses central differences to calculate the x derivative of ϕ (or ϕ_s), the pressure coefficient is not calculated on the leading and trailing edge grid points.

To facilitate the use of this program Appendix B contains a listing of a subroutine that can be used to read the output of SUPERSONIC. When this subroutine is used the number of configurations read is transferred to the main program by the variable IC. The Mach number and reduced frequencies are stored in the arrays AM(K), AOM(K) where $1 \le K \le IC$.

APPENDIX C (CONT.)

The number of grid points in the spanwise direction for the pressure/potential is stored in JP(K)/JC(K) (1 $\leq K \leq IC$). The number of grid points in the streamwise direction at the Jth spanwise

point for the pressure/potential is stored in IP1(K,J)/IP2(K,J). The value of y at the Jth spanwise position for the pressure/potential is stored in Y1(K,J)/Y2(K,K). The value of x at the Jth spanwise and Ith streamwise position for the pressure/potential is stored in X1(K,I,J) / X2(K,I,J) and finally the real and imaginary parts of the pressure coefficient and potential at the Jth spanwise and Ith streamwise grid point are stored in G(K,I,J) and F(K,I,J), where I \leq K \leq IC.

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